

1.8 Unique Compositions

Perform a composition and simplify given the two functions (either $f(g(x))$ or $g(f(x))$).

$$1) \quad \begin{aligned} g(x) &= (x-1)^3 + 1 \\ f(x) &= \sqrt[3]{x-1} + 1 \end{aligned}$$

$$2) \quad \begin{aligned} g(x) &= 1 + (x+1)^3 \\ f(x) &= \sqrt[3]{x-1} - 1 \end{aligned}$$

$$3) \quad \begin{aligned} f(x) &= 2(x+2)^5 \\ g(x) &= \frac{-4 + \sqrt[5]{16x}}{2} \end{aligned}$$

$$4) \quad \begin{aligned} g(x) &= \frac{-20 + 6x}{5} \\ f(x) &= \frac{5x + 20}{6} \end{aligned}$$

Find the inverse of each function. If you're unsure of correctness, check your work using the composition method.

5) $f(x) = \frac{4}{x} + 3$

6) $f(x) = -\frac{2}{x-2} - 2$

7) $h(x) = \sqrt[5]{x-1} - 1$

8) $g(x) = 3 + x^5$

$$9) g(x) = -2x^5$$

$$10) h(x) = \sqrt[3]{\frac{x-1}{2}}$$

CHALLENGE! Find the inverse of each function. Check your work using the composition method.

$$11) f(x) = \frac{x+2}{3x+5}$$

$$12) g(x) = \frac{7-x}{5x-2}$$

State if the given functions are inverses. Use the composition method (either $f(g(x))$ or $g(f(x))$).

13) $h(x) = 6x^3 + 3$

$$f(x) = \frac{\sqrt[3]{x-3}}{6}$$

14) $g(x) = -2(x+3)^3$

$$f(x) = \frac{-6 - \sqrt[3]{4x}}{2}$$

15) $g(x) = -2x^5 + 1$

$$f(x) = \sqrt[5]{\frac{-x+1}{2}}$$

16) $f(x) = \frac{2x-10}{3}$

$$h(x) = -\frac{5}{6}x - \frac{10}{3}$$

17) Assume two functions are inverses of each other. Given any function and its inverse, find $f(f(42))$. Explain your reasoning.

Answers to 1.8 Unique Compositions

1) Yes

$$5) f^{-1}(x) = \frac{4}{x-3}$$

$$9) g^{-1}(x) = -\frac{\sqrt[5]{16x}}{2}$$

13) No

17)

2) Yes

$$6) f^{-1}(x) = \frac{2}{x+2} + 2$$

$$10) h^{-1}(x) = 2x^3 + 1$$

14) Yes

3) Yes

$$7) h^{-1}(x) = (x+1)^5 + 1$$

$$11) f^{-1}(x) = \frac{2-5x}{3x-1}$$

15) Yes

4) Yes

$$8) g^{-1}(x) = \sqrt[5]{x-3}$$

$$12) g^{-1}(x) = \frac{2x+7}{5x+1}$$

16) No